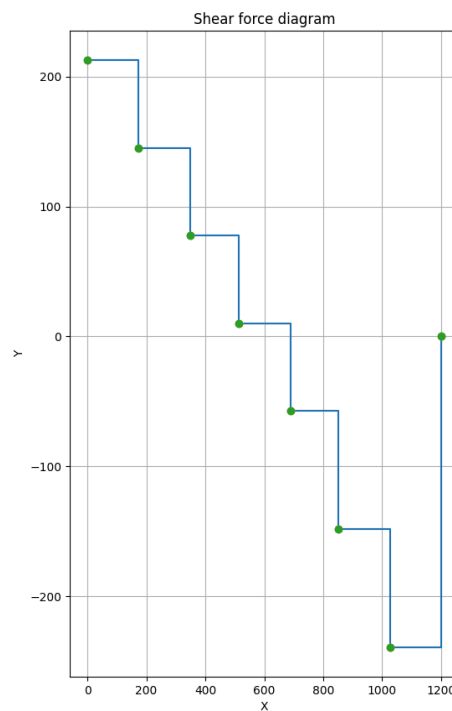
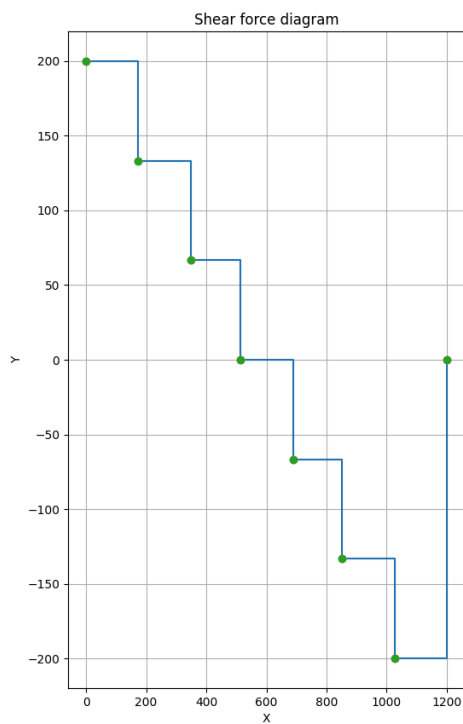


First Portion (Hand Calculations)

- FOS against failure and failure mode for Design 0 under a moving 400 N train loaded according to Load Case 1 (1.6.1)
- Any other hand calculations to determine the FOS against failure and failure mode of your final design under a train loaded according to the base case of Load Case 2 (1.6.2)

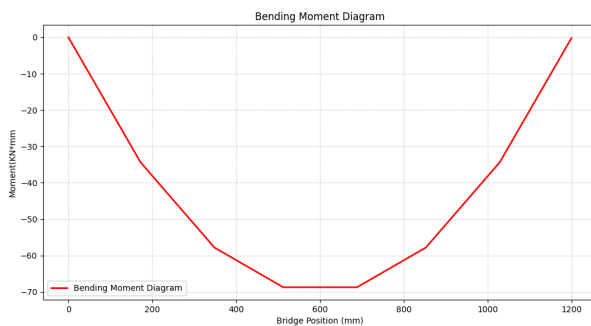
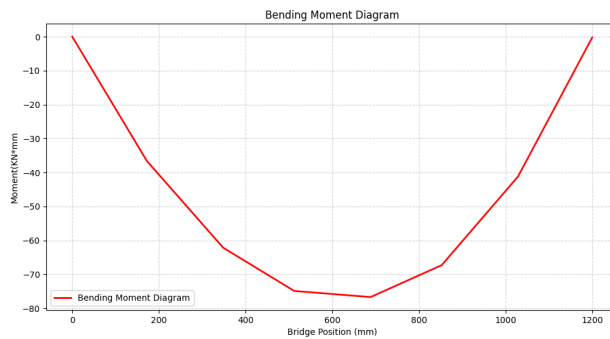
Second Portion (Programming)

- Code output for all intermediate calculations (centroidal axis location, moment of area, etc.) performed by the hand calculations of Design 0 under a moving 400 N train loaded according to Load Case 1
- SFD of Design 0 for Load Case 1 and Load Case 2 (Bobby)



(left: SFD of case one when the train is at the center. Right: SFD of case two when the train is at the middle)

- BMD of Design 0 for Load Case 1 and for your final design under Load Case 2 (Bobby)



(Up: BMD of case two when the train is at the middle; Down: BMD of case one when the train is at the center)

- Code output of all FOS values along the bridge for Load Case 1 and for your final design under Load Case 2
- Include the entire script: comments, formatting, user-defined functions; indicate installed packages (ex. NumPy) (Bobby, Candy)

1.Code for all the graphing and calculation for reaction forces, moment, and shear:
 Installed package: Matplotlib, Numpy

Code:

```
import matplotlib.pyplot as plt
import numpy as np
#Deifne support location relative to the left
length = 1200
support1 = (length-1200)/2
support2 = length-(length-1200)/2
#our case
print(support1,support2)
#calculate reaction forces based on the positions of the load: by
equilibrium of the forces and equilibrium of the moment

def reaction_calc(center_position):
    #sum of forces that's on the bridge is 0
    forcr_list2 = [] #a two dimension list, second dimension: force,loc
    loc_middle_car_force = [center_position - 88, center_position + 88] #
    [0] is on the left
```

```

loc_last_car_force = [center_position - 428, center_position - 252]
loc_first_car_force = [center_position + 252, center_position + 428]
list_load = [loc_first_car_force, loc_middle_car_force,
loc_last_car_force]
# force_dic = {"first_car": [91, loc_first_car_force], "middle_car":
[67.5, loc_middle_car_force],
#
"last_car": [67.5, loc_last_car_force]} # forces is
the sigle point force at one wheel.
force_dic = {"first_car": [67.5, loc_first_car_force], "middle_car":
[67.5, loc_middle_car_force],
"last_car": [91, loc_last_car_force]} # forces is the
sigle point force at one wheel.
# force_dic = {"first_car": [66.6, loc_first_car_force], "middle_car":
[66.6, loc_middle_car_force],
#
"last_car": [66.6, loc_last_car_force]}
#find the forces on the bridge
for i in range(0,len(list_load)):
    for j in range(0,len(list_load[i])):
        if list_load[i][j] >= 0 and list_load[i][j] <= length:

forcr_list2.append([list(force_dic.values())[i][0],list(force_dic.values(
))[i][1][j]])

#Calculate the moment at support 1
#Use the moment to get the yB second
yB = 0
for m in range(0,len(forcr_list2)):
    yB += forcr_list2[m][0]*(forcr_list2[m][1]-support1)
yB = yB/(support2-support1)
# print("yB:",yB)
#Find ya by looping all the forces and
yTotal = 0
for k in forcr_list2:
    yTotal += k[0]
# print(yTotal)
yA = yTotal-yB
# print("yA:",yA)
forcr_list2 = [[-x, y] for x, y in forcr_list2]
# print(forcr_list2)
forcr_list2.append([yA,support1])
forcr_list2.append([yB, support2])
re_list = sorted(forcr_list2,key=lambda l:l[1])
# print(re_list)
return re_list
#input is the position of the center of the train
#output will be the intensity of reaction forces, and the location of
loads and forces
def graph_shear_force(shearforce):

```

```

plt.figure(figsize=(6, 10))
x = [p[1] for p in shearforce]
y = [p[0] for p in shearforce]
plt.step(x,y, where="post")
plt.plot(x, y, 'o')
plt.plot(x, y, 'o')
plt.xlabel("X")
plt.ylabel("Y")
plt.title("Shear force diagram")
plt.grid(True)
# plt.gca().invert_yaxis() # optional: if you want y increasing
downward (like image coords)
plt.show()
def data_process(forces):
    #forces is a set of force in a sequential order from left to right. if
linear then: [force,"linear",[start,end]], if not: [force,location]
    # Calculate SFD Hard
    # calculate BMD
    # the graph of maximum moment on BMD
    # print(forces)
    shearforce = [] #two dimension list, second element is the loc, first
is the shear
    shear = 0
    for i in forces:
        # print(i)
        shear += i[0]
        shearforce.append([shear,i[1]])
    # print(shearforce)
    # graph_shear_force(shearforce)
    # graph_BMD(shearforce)
    # maximum bending moment
    Mmax = [-1000,0] # a two dimension list that the first element is the
moment the second is the position
    Moment = 0
    for i in range(1,len(shearforce)):
        distance = shearforce[i][1] - shearforce[i-1][1]
        Moment += distance* shearforce[i-1][0]/1000
        # print(Moment,distance)
        if Moment >= Mmax[0]:
            Mmax = [Moment, shearforce[i][1]]
    # print(Mmax)
    #shear max
    shearmax = [-10000000,0]
    for i in shearforce:
        if abs(i[0]) > shearmax[0]:
            shearmax = [abs(i[0]), i[1]]

    return [Mmax,shearmax]

```

```

#input: the position of forces, amount of force
#output:
#looping through every position of the train, graph each maximum moments
according to the position of the train. find the maximum moment.
def graph_max_moment(moment,loc_train_center):
    import matplotlib.pyplot as plt
    # print(moment[1])
    # Extract x and y data
    y = [p[0] for p in moment] # moment values
    x = loc_train_center # locations

    # Find maximum (x, y)
    max_y = max(y)
    i = y.index(max_y)
    max_x = x[i]
    print("max moment on bridge:",moment[i][1])
    # Print max coordinate
    print(f"Maximum moment occurs at x = {max_x}, moment = {max_y}")

    #Plot
    plt.figure(figsize=(8, 6))
    plt.plot(x, y, marker='.', linewidth=0.01)

    # Mark the max point
    plt.scatter(max_x, max_y, color='red')
    plt.text(max_x, max_y, f"({max_x:.2f}, {max_y:.2f})", color='red',
             verticalalignment='bottom')

    plt.xlabel("Train Center Location (mm)")
    plt.ylabel("Moment (kN·mm)")
    plt.title("Moment Diagram vs. Train Center Location")
    plt.grid(True)
    plt.show()

def graph_BMD(shearforce):
    Moment = 0
    Moment_list = [[0, shearforce[0][1]]]
    list_m = []
    list_x = []
    for i in range(1, len(shearforce)):
        distance = shearforce[i][1] - shearforce[i - 1][1]
        Moment += distance * shearforce[i - 1][0] / 1000
        Moment_list.append([Moment, shearforce[i][1]])
    # determine the left side moment, right side moment, expression
    print(Moment_list)
    for k in range(0,length,1):
        lf_m = 0
        lf_m_loc = 0
        rf_m = 0

```

```

    rf_m_loc = 0
    for i in range(1, len(Moment_list)):
        if Moment_list[i - 1][1] <= k and Moment_list[i - 1][1] >=
lf_m_loc:

        lf_m = Moment_list[i - 1][0]
        lf_m_loc = Moment_list[i - 1][1]
        rf_m = Moment_list[i][0]
        rf_m_loc = Moment_list[i][1]

        if rf_m_loc - lf_m_loc != 0:
            point_m = (rf_m - lf_m) / (rf_m_loc - lf_m_loc) * (k -
lf_m_loc) + lf_m
        else:
            point_m = lf_m
        # print(point_m)
        list_m.append(-point_m)
        list_x.append(k)

# Plot
plt.figure(figsize=(12, 6))
plt.plot(list_x, list_m, label="Bending Moment Diagram", color="red",
linewidth=2)
plt.xlabel("Bridge Position (mm)")
plt.ylabel("Moment (KN*mm)")
plt.title("Bending Moment Diagram")
plt.grid(True, linestyle="--", alpha=0.5)
plt.legend()
plt.show()

def plot_shear_moment_same(list_point_maxnmin_shear,
list_point_maxnmin_moment,
                           abs_shear=True):
    # Extract envelope values
    x_vals = [p[0][0] for p in list_point_maxnmin_shear] # bridge
positions

    shear_vals = [max(abs(p[0][1]), abs(p[1][1])) if abs_shear else
max(p[0][1], p[1][1])
                  for p in list_point_maxnmin_shear]

    moment_vals = [max(p[0][1], p[1][1]) for p in
list_point_maxnmin_moment]

# Plot
plt.figure(figsize=(12, 6))
plt.plot(x_vals, shear_vals, label="Shear Envelope", color="blue",
linewidth=2)
plt.plot(x_vals, moment_vals, label="Moment Envelope", color="red",
linewidth=2)

```

```

plt.xlabel("Bridge Position (mm)")
plt.ylabel("Value")
plt.title("Shear & Moment Envelope Curves on Same Plot")
plt.grid(True, linestyle="--", alpha=0.5)
plt.legend()
plt.show()

#find the envelop shear force
def graph_max_shear(shearforces,loc_train_center):
    #shearforces: two dimension vector, first element shear, second is loc
    import matplotlib.pyplot as plt
    # Extract x and y data
    y = [p[0] for p in shearforces] # shear values
    x = loc_train_center # locations

    # Find maximum (x, y)
    max_y = max(y)
    i = y.index(max_y)
    max_x = x[i]
    print("max on bridge loc:",shearforces[i][1])
    # Print max coordinate
    print(f"Maximum shear occurs at x = {max_x}, shear = {max_y}")
    # Plot
    plt.figure(figsize=(8, 6))
    plt.plot(x, y, marker='o', linewidth=1)
    # Mark the max point
    plt.scatter(max_x, max_y, color='red')
    plt.text(max_x, max_y, f"({max_x:.2f}, {max_y:.2f})", color='red',
             verticalalignment='bottom')
    plt.xlabel("Train Center Location (mm)")
    plt.ylabel("Shear Force (N)")
    plt.title("Shear Force Envelope Diagram")
    plt.grid(True)
    plt.show()

def calc_shear_along_bridge(position,forces):
    # get the shear of a specific *position* according to the forces list
    #output the shear force
    shearforce = [] # two dimension list, second element is the loc,
    first is the shear
    shear = 0
    for i in forces:
        # print(i)
        shear += i[0]
        shearforce.append([shear, i[1]])
    # print(shearforce)
    point_shear = 0
    least_left = -100000
    for i in shearforce:

```

```

        if i[1] < position and i[1]>least_left:
            least_left = i[1]
            point_shear = i[0]
            if position == 200:
                print(point_shear)
#Shear = The closest left shear
return point_shear

def cal_moment_along_bridge(position, forces):
    shearforce = [] # two dimension list, second element is the loc,
first is the shear
    shear = 0
    for i in forces:
        # print(i)
        shear += i[0]
        shearforce.append([shear, i[1]])
    Moment = 0
    Moment_list = [[0,0]]
    for i in range(1, len(shearforce)):
        distance = shearforce[i][1] - shearforce[i - 1][1]
        Moment += distance * shearforce[i - 1][0] / 1000
        Moment_list.append([Moment, shearforce[i][1]])
    #determine the left side moment, right side moment, expression
    lf_m = 0
    lf_m_loc = 0
    rf_m = 0
    rf_m_loc = 0

    for i in range(1, len(Moment_list)):
        if Moment_list[i-1][1] <= position and Moment_list[i-1][1] >=
lf_m_loc:
            lf_m = Moment_list[i-1][0]
            lf_m_loc = Moment_list[i-1][1]
            rf_m = Moment_list[i][0]
            rf_m_loc = Moment_list[i][1]

    if rf_m_loc-lf_m_loc != 0:
        point_m = (rf_m-lf_m)/(rf_m_loc-lf_m_loc)*(position -
lf_m_loc)+lf_m
    else:
        point_m = lf_m
    # print(point_m)
    return point_m
    # print(Moment, distance)
def scatter_color_by_y(data, name):
    xs = []
    ys = []

    for (x_pair, y_pair) in data:

```

```

    a, b = x_pair
    c, d = y_pair
    xs.extend([a, c])
    ys.extend([b, d])

xs = np.array(xs)
ys = np.array(ys)

# Max & Min values
y_max = np.max(ys)
y_min = np.min(ys)
# Index lists (may contain multiple points)
max_idx = np.where(ys == y_max)[0]
min_idx = np.where(ys == y_min)[0]
plt.figure(figsize=(10, 6))
# MAIN SCATTER – only scatter contributing to colorbar
sc = plt.scatter(xs, ys, c=ys, cmap='coolwarm', s=25, alpha=0.85)
plt.colorbar(sc, label=name)
# MAXIMA (highlight + annotate coordinates)
plt.scatter(xs[max_idx], ys[max_idx],
            facecolors='none', edgecolors='red',
            s=120, linewidths=2.5, label="Maxima")
for i in max_idx:
    plt.annotate(f"({xs[i]:.2f}, {ys[i]:.2f})",
                (xs[i], ys[i]),
                textcoords="offset points", xytext=(6, 6),
                fontsize=9, color='red')

# MINIMA
plt.scatter(xs[min_idx], ys[min_idx],
            facecolors='none', edgecolors='blue',
            s=120, linewidths=2.5, label="Minima")
if name != "Moment":
    # only annotate minima if NOT "Moment"
    for i in min_idx:
        plt.annotate(f"({xs[i]:.2f}, {ys[i]:.2f})",
                    (xs[i], ys[i]),
                    textcoords="offset points", xytext=(6, 6),
                    fontsize=9, color='blue')

plt.xlabel("Bridge Position (mm)")
plt.ylabel(name)
plt.title(f"{name} vs. Bridge Length")
plt.grid(True, linestyle='--', alpha=0.4)
plt.legend()

plt.show()

def plot_scaled_moment_shear(list_point_maxnmin_shear,
list_point_maxnmin_moment):

```

```

# X positions (bridge coordinates)
x_vals = [p[0][0] for p in list_point_maxnmin_shear]

# Extract shear envelope (absolute)
shear_vals = [max(abs(p[0][1]), abs(p[1][1])) for p in
list_point_maxnmin_shear]

# Extract moment envelope (positive max)
moment_vals = [max(p[0][1], p[1][1]) for p in
list_point_maxnmin_moment]
# --- Scaling ---
max_shear = max(shear_vals)
max_moment = max(moment_vals)
scale = max_shear / max_moment if max_moment != 0 else 1
moment_scaled = [m * scale for m in moment_vals]
# FIND INTERSECTIONS: shear_vals = moment_scaled
intersections = []
for i in range(1, len(x_vals)):
    x0, x1 = x_vals[i-1], x_vals[i]
    y0_s, y1_s = shear_vals[i-1], shear_vals[i]
    y0_m, y1_m = moment_scaled[i-1], moment_scaled[i]
    # Check for sign crossing (intersection between segments)
    if (y0_s - y0_m) * (y1_s - y1_m) <= 0:
        # Solve linear interpolation for intersection point
        # shear(x) = y0_s + t*(y1_s - y0_s)
        # moment(x) = y0_m + t*(y1_m - y0_m)
        # Find t where they equal
        numerator = (y0_s - y0_m)
        denominator = (y0_s - y0_m) - (y1_s - y1_m)
        if denominator != 0:
            t = numerator / denominator
            x_int = x0 + t * (x1 - x0)
            y_int = y0_s + t * (y1_s - y0_s)
            intersections.append((x_int, y_int))
# Print intersection points
print("\n=== Intersection Points (Scaled Moment = Shear) ===")
if len(intersections) == 0:
    print("No intersections found.")
else:
    for (xi, yi) in intersections:
        print(f"x = {xi:.2f} mm, value = {yi:.2f}")
plt.figure(figsize=(12, 6))
plt.plot(x_vals, shear_vals, linewidth=2.5, color="blue", label="Shear
Envelope")
plt.plot(x_vals, moment_scaled, linewidth=2.5, color="red",
label=f"Moment Envelope (scaled ×{scale:.3f})")
# Plot intersection points
for (xi, yi) in intersections:
    plt.scatter(xi, yi, color="black", s=50)

```

```

plt.text(xi, yi, f"({xi:.0f}, {yi:.1f})", fontsize=9,
color="black", ha="left", va="bottom")

plt.xlabel("Bridge Position (mm)")
plt.ylabel("Value (Scaled)")
plt.title("Scaled Moment Envelope vs. Shear Envelope (Intersections
Marked)")
plt.grid(True, linestyle="--", alpha=0.5)

# Centered legend
plt.legend(loc="upper center", bbox_to_anchor=(0.5, -0.12), ncol=2)

plt.tight_layout()
plt.show()

def return_maxnmin(list,index):
    #design for a second dimension list sorting
    a = [p[index] for p in list]
    maxa = max(a)
    mina = min(a)
    indexmax = a.index(maxa)
    indexmin = a.index(mina)
    return list[indexmax],list[indexmin]
#design aspect, inertia at different location.
list_1 = []
list_2 = []
list_loc = []
list_point_maxnmin_shear = [] #Three dimensionn list. Second dimension:
bridge loc: first: loc, second: max, third: min
list_point_maxnmin_moment = []
for j in range(0,int(support2)-int(support1),1):
    #build up the list
    list_point_maxnmin_shear.append([])
    list_point_maxnmin_moment.append([])

for i in range(-428,length+428,1):
    list_1.append(data_process(reaction_calc(i))[0])
    list_2.append(data_process(reaction_calc(i))[1])
    list_loc.append(i)
    for k in range(0,int(support2)-int(support1),1):
        #add the whole data to the list
        # print(k-1,len(list_point_maxnmin_shear))

list_point_maxnmin_shear[k].append([k,calc_shear_along_bridge(k,reaction_
calc(i))])
    list_point_maxnmin_moment[k].append([k, cal_moment_along_bridge(k,
reaction_calc(i))])

for m in range(0,len(list_point_maxnmin_shear)):

```

```

    list_point_maxnmin_shear[m] =
return_maxnmin(list_point_maxnmin_shear[m],1)
    list_point_maxnmin_moment[m] =
return_maxnmin(list_point_maxnmin_moment[m], 1)
# print(list_point_maxnmin_shear)
scatter_color_by_y(list_point_maxnmin_shear,"Shear Force")
scatter_color_by_y(list_point_maxnmin_moment,"Moment")
# # print(len(list_1),len(list_2))
graph_max_moment(list_1,list_loc)
graph_max_shear(list_2,list_loc)
plot_shear_moment_same(list_point_maxnmin_shear,
list_point_maxnmin_moment)
plot_scaled_moment_shear(list_point_maxnmin_shear,
list_point_maxnmin_moment)

# print(graph_shear_along_bridge(600,reaction_calc(800)))
# print(data_process(reaction_calc(600))[0])

```

2. Code for calculating the FOS (math was imported)

```

import math

# 3. Maximum Moment and Shear Force
M =
V =

# 4. Bridge Geometry (Design Parameters)
t =
b1 =
b2 =
b3_4 = t
b5_6 =
h1 =
h2 = t
h_bot =
h3_4 = h_bot - t
h5_6 = t
a =

# 5. Calculate Cross-sectional Geometric Properties (y bar, Q, I)
def cross_section():
    A1 = b1 * h1
    A2 = b2 * h2
    A3_4 = 2 * h3_4 * b3_4
    A5_6 = 2 * h5_6 * b5_6
    # total area
    At = A1 + A2 + A3_4 + A5_6

```

```

y1 = h_bot + h1/2
y2 = h2/2
y3_4 = h2 + h3_4/2
y5_6 = h_bot - h5_6 + h5_6/2
# y bar
y_bar = (A1 * y1 + A2 * y2 + A3_4 * y3_4 + A5_6 * y5_6)/At
# Second Moment of Inertia
I1 = (b1 * (h1) ** 3)/12
I2 = (b2 * (h2) ** 3)/12
I3_4 = 2 * ((b3_4 * h3_4 ** 3)/12)
I5_6 = 2 * (b5_6 * h5_6 ** 3/12)
It1 = I1 + I2 + I3_4 + I5_6
# Distance of Individual Distance to y bar
d1 = abs(y_bar - y1)
d2 = abs(y_bar - y2)
d3_4 = abs(y_bar - y3_4)
d5_6 = abs(y_bar - y5_6)
# Aidi^2
Ad1 = A1 * d1 ** 2
Ad2 = A2 * d2 ** 2
Ad3_4 = A3_4 * d3_4 ** 2
Ad5_6 = A5_6 * d5_6 ** 2
Adt = Ad1 + Ad2 + Ad3_4 + Ad5_6
# Total Moment of Inertia
It2 = It1 + Adt
# Q at centroidal axes
Q_cent = b2 * h2 * (y_bar - h2/2) + 2 * b3_4 * (y_bar - h2) * (y_bar - h2)/2
# Q at glue location
Q_glue = b1 * h1 * (h_bot + h1/2 - y_bar)
return y_bar, Q_cent, Q_glue, It2, At

# 6. Calculate Applied Stresses
def applied_stress(y_bar, Q_cent, Q_glue, It2):
    y_top = h_bot + h1 - y_bar
    y_bottom = y_bar
    # Max Compressive Stress (Top)
    s_comp = (M * y_top) / It2
    # Max Tensile Stress (Bottom)
    s_tens = (M * y_bottom) / It2
    # Max Shear Stress (at centroid)
    b_cent = 2 * b3_4
    tau_cent = (V * Q_cent)/(It2 * b_cent)

```

```

# Max Shear Stress (at glue location)
b_glue = 2 * (b5_6)
tau_glue = (V * Q_glue)/(It2 * b_glue)
return s_comp, s_tens, tau_cent, tau_glue, y_top

# 7. Calculate material/thin plate buckling capacities
def plate_buckling(y_bar, Q, It2):
    Vm = 0.2
    E = 4000
    # Case 1 buckling (compressive flange between the webs)
    s_buck1 = (4 * (math.pi) ** 2 * E) * (h1 / b2) ** 2 / (12 * (1 - Vm ** 2))
    # Case 2 buckling (tips of the compressive flange)
    s_buck2 = (0.425 * (math.pi) ** 2 * E) * (h1 / ((b1 - b2)/2)) ** 2 / (12 * (1 - Vm
** 2))
    # Case 3 buckling (webs due to flexural stresses)
    s_buck3 = (6 * (math.pi) ** 2 * E) * (b3_4 / (h_bot - y_bar)) ** 2 / (12 * (1 - Vm
** 2))
    # Case 4 buckling (shear buckling of the webs)
    tau_buckV = ((5 * (math.pi) ** 2 * E) * ((b3_4/h_bot) ** 2 + (t/a) ** 2)) / (12 * (1
- Vm ** 2))
    return s_buck1, s_buck2, s_buck3, tau_buckV

# 8. FOS
def factor_of_safety(s_comp, s_tens, tau_cent, tau_glue, s_buck1, s_buck2, s_buck3,
tau_buckV):
    fos_tens = 30/s_tens
    fos_comp = 6 / s_comp
    fos_shear = 4 / tau_cent
    fos_glue = 2 / tau_glue
    fos_buck1 = s_buck1 / s_comp
    fos_buck2 = s_buck2 / s_comp
    fos_buck3 = s_buck3 / s_comp
    fos_buckV = tau_buckV / tau_cent
    return fos_tens, fos_comp, fos_shear, fos_glue, fos_buck1, fos_buck2, fos_buck3,
fos_buckV

# 9. Min FOS and the failure load Pfail
def min_FOS(fos_tens, fos_comp, fos_shear, fos_glue, fos_buck1, fos_buck2, fos_buck3,
fos_buckV, s_buck1, y_top):
    min_FOS = min(fos_tens, fos_comp, fos_shear, fos_glue, fos_buck1, fos_buck2,
fos_buck3, fos_buckV)
    Pf = 452 * min_FOS

```

```

    return min_FOS, Pf

# --- Cross-section properties ---
y_bar, Q_cent, Q_glue, It2, At = cross_section()

# --- Applied stresses ---
s_comp, s_tens, tau_cent, tau_glue, y_top = applied_stress(y_bar, Q_cent, Q_glue, It2)

# --- Buckling ---
s_buck1, s_buck2, s_buck3, tau_buckV = plate_buckling(y_bar, Q_cent, It2)

# --- Factor of Safety ---
fos_tens, fos_comp, fos_shear, fos_glue, fos_buck1, fos_buck2, fos_buck3, fos_buckV = \
    factor_of_safety(s_comp, s_tens, tau_cent, tau_glue, s_buck1, s_buck2, s_buck3,
tau_buckV)

# --- Min FOS & Failure Load ---
min_fos, Pf = min_FOS(fos_tens, fos_comp, fos_shear, fos_glue, fos_buck1, fos_buck2,
fos_buck3, fos_buckV, s_buck1, y_top)

# --- Create dictionary of all variables ---
all_values = {
    # Load & Geometry
    "M": M,
    "V": V,
    # Cross-section
    "y_bar": y_bar,
    "Q_cent": Q_cent,
    "Q_glue": Q_glue,
    "I": It2,
    "Area": At,
    # Applied Stresses
    "s_comp": s_comp,
    "s_tens": s_tens,
    "tau_cent": tau_cent,
    "tau_glue": tau_glue,
    "y_top": y_top,
    # Buckling
    "s_buck1": s_buck1,
    "s_buck2": s_buck2,
    "s_buck3": s_buck3,

```

```

"tau_buckV": tau_buckV,
# Factor of Safety
"fos_tens": fos_tens,
"fos_comp": fos_comp,
"fos_shear": fos_shear,
"fos_glue": fos_glue,
"fos_buck1": fos_buck1,
"fos_buck2": fos_buck2,
"fos_buck3": fos_buck3,
"fos_buckV": fos_buckV,
# Min FOS & Failure Load
"min_FOS": min_fos,
"Failure_Load": Pf}

# --- Print all variables ---
print("=== All Calculated Values ===")
for name, value in all_values.items():
    print(f"{name}: {value:.3f}")

```

Hand calculation of design 0 (load case 1)

$A_1 = 101.6$
 $y_1 = 46.55$
 $A_2 = 95.23$
 $y_2 = 33.77$
 $A_3 = 93.73$
 $y_3 = 38.77$

$A_{tot} = 419.1$
 $\bar{y} = 41.4$ (from bot edge)

$I = \frac{bh^3}{12}$ (section 1, 2, 3, 4)
 $I = 0.418 \times 10^6 \text{ mm}^4$
 $\approx 418,000 \text{ mm}^4$

$Q_T = \frac{VQ}{Ib}$
 $Q_T = (173.3 \times 96.9 - 91.08) + 2(1.73 \times (26.27 - 91.08) - 41.08)$
 $V = 250.4$
 $Q_T = 6,700 \text{ mm}^3$
 $b = 2.34$
 $b = 2 \times 1.27$ (2 webs)
 $J = 918 \times 10^6 \text{ mm}^4$
 $\tau_{xy} = 1.940 \text{ MPa}$

GLUE

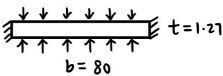
$Q = 4,340$
 $b = (\text{Assume } 5 \text{ mm}) = 2 \times 0.5 + 2.9 = 3.9$
 $\tau = \frac{Q}{bI} = \frac{4340}{(3.9 \times 10^6)(10)} = 0.111 \text{ MPa}$

MAT bending stress
 $\sigma_c = \frac{My}{I} = \frac{(68996)(91.27)}{418 \times 10^4} = 5.74$
 $\sigma_c = \frac{My}{I} = \frac{(68996)(41.4)}{418 \times 10^4} = 6.87$

FOS
 $FOS_c = \frac{\sigma_{allow}}{\sigma} = \frac{6}{5.74} = 1.045$
 $FOS_t = \frac{30}{6.87} = 4.37$
 $FOS_{glue} = \frac{\tau_{allow}}{\tau} = \frac{1.94}{0.111} = 17.48$
 $FOS_{shear} = \frac{4}{1.960} = 2.04$

Specified dimensions	32" x 48" x 0.007" (813 mm x 1,219 mm x 0.177 mm)
Tensile strength, σ_t	30 MPa
Compressive strength, σ_c	3,300 psi
Shear strength, τ_v	1,500 psi
Modulus of elasticity, E_c	1,000 MPa
Density ratio, γ_c	1.2
Contractor Comment	Shear strength, τ_v Up to 2 MPa if properly coated!

Case 1 (buckling of the compressive flange between the webs)

$$\sigma_{crit} = \frac{4\pi^2 E}{12(1-\mu^2)} \left(\frac{t}{b}\right)^2$$


$$= 3.45 \text{ MPa}$$

$$FOS = \frac{\sigma_{crit}}{\sigma_c} = \frac{3.45}{5.94} = 0.581$$

case 2 (buckling of the tips of the compressive flange)

$$\sigma_{crit} = \frac{0.425 \pi^2 E}{12(1-\mu^2)} \left(\frac{t}{b}\right)^2$$


$$= 23.5 \text{ MPa}$$

$$FOS = \frac{\sigma_{crit}}{\sigma_c} = \frac{23.5}{5.94} = 3.96$$

Case 3 (buckling of the webs due to the flexural stresses)

$$\sigma_{crit} = \frac{6 \pi^2 E}{12(1-\mu^2)} \left(\frac{t}{b}\right)^2$$


$$= 29.4 \text{ MPa}$$

$$FOS = \frac{\sigma_{crit}}{\sigma_c} = \frac{29.4}{5.94} = 4.95$$

case 4 (shear buckling of the web)

$$\tau_{crit} = \frac{5 \pi^2 E}{12(1-\mu^2)} \left(\left(\frac{t}{h}\right)^2 + \left(\frac{t}{a}\right)^2 \right)$$

$h = 75$
 $a = 400$
 $t = 1.27$

$$= 5.09 \text{ MPa}$$

$$FOS = \frac{\tau_{crit}}{\tau_{cent}} = \frac{5.09}{1.44} = 3.53$$

FOS_{tens} = 4.45

FOS_{comp} = 1.01

FOS_{flex_buck_1} = 0.581

FOS_{flex_buck_2} = 3.96

FOS_{flex_buck_3} = 4.95

FOS_{shear} = 2.77

FOS_{glue} = 7.40

FOS_{shear_buck} = 3.53

Minimum FOS: FOS_{flex_buck_1}

Failure Mode: Case 1 buckling of the compressive flange between the webs

DESIGN 0 Calculation: (LOAD CASE 1)

M: 69380.000

V: 256.740

y_{bar}: 41.431

Q_{cent}: 6193.283

Q_{glue}: 4343.896

I: 418352.209

Area: 428.574

s_{comp}: 5.778

s_{tens}: 6.871

tau_{cent}: 1.496

tau_{glue}: 0.267

y_top: 34.839
s_buck1: 3.455
s_buck2: 23.491
s_buck3: 29.430
tau_buckV: 5.086
fos_tens: 4.366
fos_comp: 1.038
fos_shear: 2.673
fos_glue: 7.502
fos_buck1: 0.598
fos_buck2: 4.066
fos_buck3: 5.094
fos_buckV: 3.399
min_FOS: 0.598
Failure_Load: 239.165

DESIGN 0 (LOAD CASE 2):

M: 78100.000
V: 304.100
y_bar: 41.431
Q_cent: 6193.283
Q_glue: 4343.896
I: 418352.209
Area: 428.574
s_comp: 6.504
s_tens: 7.735
tau_cent: 1.772
tau_glue: 0.316
y_top: 34.839
s_buck1: 3.455
s_buck2: 23.491
s_buck3: 29.430
tau_buckV: 5.086
fos_tens: 3.879
fos_comp: 0.923
fos_shear: 2.257
fos_glue: 6.334
fos_buck1: 0.531
fos_buck2: 3.612
fos_buck3: 4.525
fos_buckV: 2.870
min_FOS: 0.531
Failure_Load: 240.082

ITERATION 1: (DOUBLE THICKNESS)

M: 78100.000
V: 304.100
y_bar: 49.540
Q_cent: 7927.874
Q_glue: 6789.380
I: 541652.987
Area: 555.574
s_comp: 4.037
s_tens: 7.143
tau_cent: 1.752
tau_glue: 0.381
y_top: 28.000
s_buck1: 13.818
s_buck2: 93.964
s_buck3: 51.163
tau_buckV: 5.086
fos_tens: 4.200
fos_comp: 1.486
fos_shear: 2.283
fos_glue: 5.247
fos_buck1: 3.423
fos_buck2: 23.274
fos_buck3: 12.673
fos_buckV: 2.902
min_FOS: 1.486
Failure_Load: 671.745

Iteration 2 (increase height to 80 mm)

M: 78100.000
V: 208.300
y_bar: 52.512
Q_cent: 8605.302
Q_glue: 7304.636
I: 624304.226
Area: 568.274
s_comp: 3.757
s_tens: 6.569
tau_cent: 1.130
tau_glue: 0.244
y_top: 30.028
s_buck1: 13.818
s_buck2: 93.964

s_buck3: 43.890
tau_buckV: 4.491
fos_tens: 4.567
fos_comp: 1.597
fos_shear: 3.539
fos_glue: 8.206
fos_buck1: 3.678
fos_buck2: 25.014
fos_buck3: 11.684
fos_buckV: 3.973
min_FOS: 1.597
Failure_Load: 721.943

ITERATION 3 (DOUBLE HEIGHT TO 160mm; decrease diaphragm spacing to 200 > 5 diaphragms):

M: 78100.000
V: 304.100
y_bar: 97.944
Q_cent: 21755.711
Q_glue: 16084.898
I: 2996000.654
Area: 771.474
s_comp: 1.684
s_tens: 2.553
tau_cent: 0.869
tau_glue: 0.163
y_top: 64.596
s_buck1: 13.818
s_buck2: 93.964
s_buck3: 8.612
tau_buckV: 1.770
fos_tens: 11.750
fos_comp: 3.563
fos_shear: 4.601
fos_glue: 12.250
fos_buck1: 8.206
fos_buck2: 55.802
fos_buck3: 5.114
fos_buckV: 2.036
min_FOS: 2.036
Failure_Load: 920.477

ITERATION 3 (decrease diaphragm spacing to 120 > 9 diaphragms):

M: 78100.000
V: 208.300
y_bar: 98.345
Q_cent: 21895.402
Q_glue: 15982.841
I: 3015040.697
Area: 776.554
s_comp: 1.663
s_tens: 2.547
tau_cent: 0.596
tau_glue: 0.079
y_top: 64.195
s_buck1: 13.818
s_buck2: 93.964
s_buck3: 8.724
tau_buckV: 2.999
fos_tens: 11.776
fos_comp: 3.608
fos_shear: 6.717
fos_glue: 25.358
fos_buck1: 8.310
fos_buck2: 56.508
fos_buck3: 5.247
fos_buckV: 5.035
min_FOS: 3.608
Failure_Load: 1630.923

Thought process of optimizing:

SECTION 1 & 2 (two ends of the bridge): (h_bot = 100)

M: 53700.000
V: 302.300
y_bar: 64.490
Q_cent: 11563.586
Q_glue: 9342.098
I: 1031494.046
Area: 624.154
s_comp: 1.981
s_tens: 3.357
tau_cent: 1.334
tau_glue: 0.196
y_top: 38.050
s_buck1: 13.818
s_buck2: 93.964

s_buck3: 26.301
tau_buckV: 3.843
fos_tens: 8.936
fos_comp: 3.029
fos_shear: 2.998
fos_glue: 10.227
fos_buck1: 6.976
fos_buck2: 47.435
fos_buck3: 13.277
fos_buckV: 2.880
min_FOS: 2.880
Failure_Load: 1301.976

SECTION 3 (middle of the bridge): ($h_{bot} = 120$) two LAYERS for cross-section

M: 78100.000
V: 208.300
y_bar: 75.969
Q_cent: 14740.356
Q_glue: 11506.544
I: 1556670.695
Area: 674.954
s_comp: 2.337
s_tens: 3.811
tau_cent: 0.777
tau_glue: 0.110
y_top: 46.571
s_buck1: 13.818
s_buck2: 93.964
s_buck3: 17.106
tau_buckV: 2.999
fos_tens: 7.871
fos_comp: 2.568
fos_shear: 5.151
fos_glue: 18.185
fos_buck1: 5.914
fos_buck2: 40.215
fos_buck3: 7.321
fos_buckV: 3.862
min_FOS: 2.568
Failure_Load: 1160.691

Three layers:

M: 78100.000
V: 208.300

y_bar: 83.444
Q_cent: 16989.276
Q_glue: 14653.491
I: 1794880.965
Area: 801.954
s_comp: 1.756
s_tens: 3.631
tau_cent: 0.776
tau_glue: 0.121
y_top: 40.366
s_buck1: 31.091
s_buck2: 211.420
s_buck3: 24.817
tau_buckV: 2.999
fos_tens: 8.262
fos_comp: 3.416
fos_shear: 5.153
fos_glue: 16.465
fos_buck1: 17.702
fos_buck2: 120.370
fos_buck3: 14.130
fos_buckV: 3.863
min_FOS: 3.416
Failure_Load: 1544.055

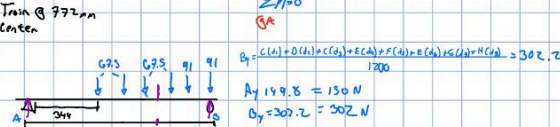
HAND CALCULATIONS FOR FINAL DESIGN

Hand Calculations For Final Design

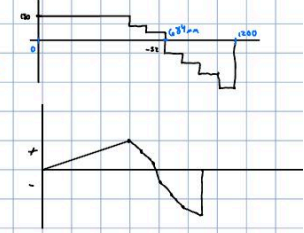
(Two Different Cross Sections through the bridge)



Train @ 972 mm Center



$\sum M = 0$
OK



For Sections 1 and 3 (height of the web: 100 mm)

Max Moment: 302.5 N·m
Max Shear: 302.5 N
 $\bar{y} = 64.2$ mm
 $I = 1025269$ mm⁴

Centroid: $\tau_{xy} = \frac{VA}{I_s}$
 $Q = 11788$
 $b = (1.27 \times 2)$
 $\tau_{xy} = 1.33$ MPa

Shear: $\tau_{shear} = \frac{VA}{I_s}$
 $Q = 9915$
 $b = (1.27)$
 $\tau_{shear} = 0.2799$

MAX bending stress
 $\sigma_c = \frac{My}{I} = \frac{(302.5)(38.3)}{1025269}$
 $\sigma_c = 2$

$\sigma_c = \frac{My}{I} = \frac{(302.5)(64.2)}{1025269}$
 $\sigma_c = 3.36$

FOS $\frac{\sigma_{allowable}}{\sigma_{max}}$ or $\frac{F_{allowable}}{F_{max}}$

$FOS_c = \frac{6}{2} = 3$
 $FOS_t = \frac{30}{3.36} = 8.94$
 $FOS_{shear} = \frac{1}{0.2799} = 3.57$
 $FOS_{shear} = \frac{4}{1.33} = 3$

CASE 7 buckling of the compressive flange between the webs
 $\frac{4\pi^2 E (1000)}{12(1-0.2^2)} \left(\frac{127+2}{80}\right)^2 = FOS \frac{15.81}{2} = 6.9$

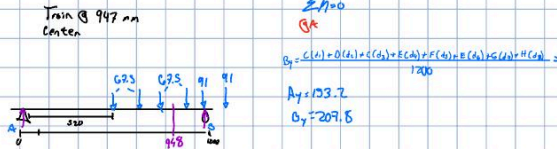
CASE 2 buckling of the tips of the compressive flange
 $\frac{0.425 \pi^2 E}{12(1-0.2^2)} \left(\frac{t}{b}\right)^2 = FOS \frac{13.94}{2} = 46.9$
 $t = 1.29 \times 2$
 $b = 10$

CASE 3 buckling of the webs due to flexural stresses
 $\frac{6\pi^2 E}{12(1-0.2^2)} \left(\frac{t}{b}\right)^2 = FOS \frac{25.8}{2} = 12.9$
 $b = 38.3$
 $t = 1.29$

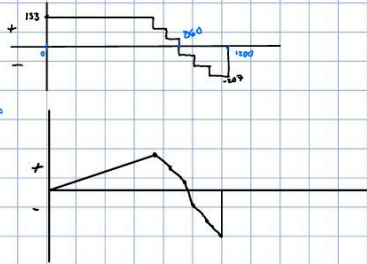
CASE 4 shear buckling of the web
 $\frac{5\pi^2 E}{12(1-0.2^2)} \left[\left(\frac{t}{h}\right)^2 + \left(\frac{t}{a}\right)^2\right] = FOS \frac{3.84}{1.33} = 2.89$
 $t = 1.29$
 $h = 100$
 $a = 160$ (Max spacing between diaphragms)

For Section 3 (height of the web: 120 mm)

Train @ 947 mm Center



$\sum M = 0$
OK



Max Moment: 208.3 N·m
Max Shear: 208.3 N
 $\bar{y} = 75.61$ mm
 $I = 1547030$ mm⁴

Centroid: $\tau_{xy} = \frac{VA}{I_s}$
 $Q = 11640$
 $b = (1.27 \times 2)$
 $\tau_{xy} = 0.7794$ MPa

Shear: $\tau_{shear} = \frac{VA}{I_s}$
 $Q = 8240$
 $b = (1.27)$
 $\tau_{shear} = 0.110$ MPa

MAX bending stress
 $\sigma_c = \frac{My}{I} = \frac{(208.3)(46.9)}{1547030}$
 $\sigma_c = 2.37$

$\sigma_c = \frac{My}{I} = \frac{(208.3)(75.6)}{1547030}$
 $\sigma_c = 3.32$

FOS $\frac{\sigma_{allowable}}{\sigma_{max}}$ or $\frac{F_{allowable}}{F_{max}}$

$FOS_c = \frac{6}{2.37} = 2.53$
 $FOS_t = \frac{30}{3.32} = 9.06$
 $FOS_{shear} = \frac{1}{0.110} = 9.09$
 $FOS_{shear} = \frac{4}{0.774} = 5.16$

CASE 7 buckling of the compressive flange between the webs
 $\frac{4\pi^2 E (1000)}{12(1-0.2^2)} \left(\frac{127+2}{80}\right)^2 = FOS \frac{15.8}{2.37} = 6.9$

CASE 2 buckling of the tips of the compressive flange
 $\frac{0.425 \pi^2 E}{12(1-0.2^2)} \left(\frac{t}{b}\right)^2 = FOS \frac{13.94}{2.37} = 59.6$
 $t = 1.29 \times 2$
 $b = 10$

CASE 3 buckling of the webs due to flexural stresses
 $\frac{6\pi^2 E}{12(1-0.2^2)} \left(\frac{t}{b}\right)^2 = FOS \frac{16.85}{2.37} = 9.11$
 $b = 44.36$
 $t = 1.29$

CASE 4 shear buckling of the web
 $\frac{5\pi^2 E}{12(1-0.2^2)} \left[\left(\frac{t}{h}\right)^2 + \left(\frac{t}{a}\right)^2\right] = FOS \frac{2.94}{0.774} = 3.87$
 $t = 1.29$
 $h = 120$
 $a = 160$ (Max spacing between diaphragms)